

2022Call6.

(1) Q1

CLOZE

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{a}{b}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Complete the formulae.

$$(x+1)^{\frac{1}{2}} = \boxed{a} + \frac{\boxed{b}}{\boxed{c}}x + \frac{\boxed{d}}{\boxed{e}}x^2 + \frac{\boxed{f}}{\boxed{g}}x^3 \text{ as } x \rightarrow 0.$$

a:

NUMERICAL

1 point

1 ✓

b:

NUMERICAL

1 point

1 ✓

c:

NUMERICAL

1 point

2 ✓

d:

NUMERICAL

1 point

-1 ✓

e:

NUMERICAL

1 point

8 ✓

f:

NUMERICAL

1 point

1 ✓

g:

NUMERICAL

2 points

16 ✓

$$(x-1)\exp x = \boxed{h} + \boxed{i}x + \frac{\boxed{j}}{\boxed{k}}x^2 + \frac{\boxed{l}}{\boxed{m}}x^3 + o(x^3) \text{ as } x \rightarrow 0.$$

\boxed{h} :

NUMERICAL

1 point

-1 ✓

\boxed{i} :

NUMERICAL

1 point

0 ✓

\boxed{j} :

NUMERICAL

1 point

1 ✓

\boxed{k} :

NUMERICAL

2 points

2 ✓

\boxed{l} :

NUMERICAL

1 point

1 ✓

\boxed{m} :

NUMERICAL

2 points

3 ✓

$$\sin(2x^2) \cdot x = \boxed{o} + \boxed{p}x + \boxed{q}x^2 + \boxed{r}x^3 + o(x^3) \text{ as } x \rightarrow 0.$$

\boxed{o} :

NUMERICAL

3 points

0 ✓

\boxed{p} :

NUMERICAL

1 point

0 ✓

\boxed{q} :

NUMERICAL

1 point

0 ✓

\boxed{r} :

NUMERICAL

3 points

2 ✓

For various $\alpha, \beta \in \mathbb{R}$, study the limit:

$$\lim_{x \rightarrow 0} \frac{(x+1)^{\frac{1}{2}} + (x-1) \exp x + \alpha x + \beta x^2}{\sin(2x^2) \cdot x}.$$

This limit converges for $\alpha = \frac{s}{t}, \beta = \frac{u}{v}$.

s:

NUMERICAL

4 points

-1 ✓

t:

NUMERICAL

4 points

2 ✓

u:

NUMERICAL

4 points

-3 ✓

v:

NUMERICAL

4 points

8 ✓

In that case, the limit is $\frac{w}{x}$.

w:

NUMERICAL

4 points

19 ✓

x:

NUMERICAL

4 points

96 ✓

(2) Q1

CLOZE

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{a}{b}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Complete the formulae.

$$(3x+1)^{\frac{1}{2}} = \frac{a}{c} + \frac{b}{c}x + \frac{d}{e}x^2 + \frac{f}{g}x^3 \text{ as } x \rightarrow 0.$$

a:	
NUMERICAL	1 point
1 ✓	
b:	
NUMERICAL	1 point
3 ✓	
c:	
NUMERICAL	1 point
2 ✓	
d:	
NUMERICAL	1 point
-9 ✓	
e:	
NUMERICAL	1 point
8 ✓	
f:	
NUMERICAL	1 point
27 ✓	
g:	
NUMERICAL	2 points
16 ✓	

$$(x - 1) \exp x = \boxed{h} + \boxed{i}x + \frac{\boxed{j}}{\boxed{k}}x^2 + \frac{\boxed{l}}{\boxed{m}}x^3 + o(x^3) \text{ as } x \rightarrow 0.$$

h:	
NUMERICAL	1 point
-1 ✓	
i:	
NUMERICAL	1 point
0 ✓	
j:	
NUMERICAL	1 point
1 ✓	
k:	
NUMERICAL	2 points

2 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">1:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">1 point</div> </div>	
1 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">m:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">2 points</div> </div>	
3 ✓	

$$\sin(x^2) \cdot x = \boxed{o} + \boxed{p}x + \boxed{q}x^2 + \boxed{r}x^3 + o(x^3) \text{ as } x \rightarrow 0.$$

<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">o:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">3 points</div> </div>	
0 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">p:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">1 point</div> </div>	
0 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">q:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">1 point</div> </div>	
0 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">r:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">3 points</div> </div>	
1 ✓	

For various $\alpha, \beta \in \mathbb{R}$, study the limit:

$$\lim_{x \rightarrow 0} \frac{(3x+1)^{\frac{1}{2}} + (x-1)\exp x + \alpha x + \beta x^2}{\sin(x^2) \cdot x}.$$

This limit converges for $\alpha = \frac{\boxed{s}}{\boxed{t}}, \beta = \frac{\boxed{u}}{\boxed{v}}$.

<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">s:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">4 points</div> </div>	
-3 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">t:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">4 points</div> </div>	
2 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">u:</div>	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px;">NUMERICAL</div> <div style="border: 1px solid black; padding: 2px 5px;">4 points</div> </div>	
5 ✓	
<div style="border: 1px solid black; display: inline-block; padding: 2px 5px;">v:</div>	

NUMERICAL 4 points

8 ✓

In that case, the limit is $\frac{W}{X}$.

W:

NUMERICAL 4 points

97 ✓

X:

NUMERICAL 4 points

48 ✓

(3) Q2

CLOZE 0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the

answer boxes (such as $\frac{a}{b}$) have ambiguity, the negative sign

should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us study the following series $\sum_{n=0}^{\infty} \frac{4^n - 1}{n^2 + 3} (x + 1)^{2n}$, with various x .

This series makes sense also for $x \in \mathbb{C}$. For $x = i$, calculate the partial sum $\sum_{n=0}^2 \frac{4^n - 1}{n^2 + 3} (x + 1)^{2n} = \frac{a}{b} + \frac{c}{d}i$.

a:

NUMERICAL 1 point

-60 ✓

b:

NUMERICAL 1 point

7 ✓

c:

NUMERICAL 1 point

3 ✓

d:

NUMERICAL 1 point

2 ✓

In order to use the ratio test for $x \in \mathbb{R}$, we put $a_n = \frac{4^n - 1}{n^2 + 3}(x + 1)^{2n}$. Complete the formula.

$$\lim_{n \rightarrow \infty} \frac{a_{n+1}}{a_n} = \boxed{\text{e}} \|x + \boxed{\text{g}}\|^{\boxed{\text{h}}}$$

$\boxed{\text{e}}$:

NUMERICAL

2 points

4 ✓

$\boxed{\text{f}}$:

NUMERICAL

1 point

1 ✓

$\boxed{\text{g}}$:

NUMERICAL

1 point

2 ✓

Therefore, by the ratio test, the series converges absolutely for

MULTI

8 points

Single

- all x .
- $-3 < x < -1$.
- $-3 < x < 1$.
- $-2 < x < 2$.
- $\frac{1}{2} < x < \frac{3}{2}$.
- $-\frac{3}{2} < x < -\frac{1}{2}$. ✓
- $-1 < x < 1$.
- $-1 < x < 3$.
- $-\frac{1}{2} < x < \frac{1}{2}$.
- $x = 0$.
- $1 < x < 3$.

For the case $x = -\frac{3}{2}$, the series

MULTI

4 points

Single

Shuffle

- converges absolutely. ✓
- converges but not absolutely.
- diverges.

For the case $x = 1$, the series

MULTI

4 points

Single

Shuffle

- converges absolutely.
- converges but not absolutely.
- diverges. ✓

(4) Q2

CLOZE

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\boxed{a}}{\boxed{b}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us study the following series $\sum_{n=0}^{\infty} \frac{4^n - 1}{n^2 + 3} (x - 1)^{2n}$, with various x .

This series makes sense also for $x \in \mathbb{C}$. For $x = i$, calculate the partial sum $\sum_{n=0}^2 \frac{4^n - 1}{n^2 + 3} (x - 1)^{2n} = \frac{\boxed{a}}{\boxed{b}} + \frac{\boxed{c}}{\boxed{d}} i$.

\boxed{a} :

NUMERICAL 1 point

-60 ✓

\boxed{b} :

NUMERICAL 1 point

7 ✓

\boxed{c} :

NUMERICAL 1 point

-3 ✓

\boxed{d} :

NUMERICAL 1 point

2 ✓

In order to use the ratio test for $x \in \mathbb{R}$, we put $a_n = \frac{4^n - 1}{n^2 + 3} (x - 1)^{2n}$. Complete the formula.

$$\lim_{n \rightarrow \infty} \frac{a_{n+1}}{a_n} = \boxed{e} |x + \boxed{g}|^{\boxed{h}}$$

\boxed{e} :

NUMERICAL 2 points

4 ✓

\boxed{f} :

NUMERICAL 1 point

-1 ✓

\boxed{g} :

NUMERICAL 1 point

2 ✓

Therefore, by the ratio test, the series converges absolutely for

- all x .
- $-3 < x < -1$.
- $-3 < x < 1$.
- $-2 < x < 2$.
- $\frac{1}{2} < x < \frac{3}{2}$. ✓
- $-\frac{3}{2} < x < -\frac{1}{2}$.
- $-1 < x < 1$.
- $-1 < x < 3$.
- $-\frac{1}{2} < x < \frac{1}{2}$.
- $x = 0$.
- $1 < x < 3$.

For the case $x = -\frac{3}{2}$, the series

- converges absolutely.
- converges but not absolutely.
- diverges. ✓

For the case $x = 1$, the series

- converges absolutely. ✓
- converges but not absolutely.
- diverges.

(5) **Q3**

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the

answer boxes (such as $\frac{a}{b}$) have ambiguity, the negative sign

should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us consider the following function

$$f(x) = \log \left(\frac{x}{x^2 + 1} \right).$$

The function $f(x)$ is not defined on the whole real line \mathbb{R} . Choose all the points that are **not** in the natural domain of $f(x)$.

- -2 ✓
- -1 ✓
- $-\frac{1}{2}$ ✓
- 0 ✓
- $\frac{1}{2}$ (-100%)
- 1 (-100%)
- 2 (-100%)

Choose all asymptotes of $f(x)$.

☐ MULTI ☐ 4 points ☐ Single

- $y = -1$ (-100%)
- $y = -\frac{1}{2}$ (-100%)
- $y = 0$ (-100%)
- $y = \frac{1}{2}$ (-100%)
- $y = 2$ (-100%)
- $x = -2$ (-100%)
- $x = -1$ (-100%)
- $x = -\frac{1}{2}$ (-100%)
- $x = 0$ ✓
- $x = \frac{1}{2}$ (-100%)
- $x = 1$ (-100%)
- $x = 2$ (-100%)
- $y = -x$ (-100%)
- $y = x$ (-100%)

One has

$$f'(2) = \frac{\boxed{a}}{\boxed{b}}.$$

:

☐ NUMERICAL ☐ 4 points

✓

:

☐ NUMERICAL ☐ 4 points

✓

The function $f(x)$ has stationary point(s) in the domain

:

☐ NUMERICAL ☐ 4 points

✓

Choose the behaviour of $f(x)$ in the interval $(0, 2)$.

☐ MULTI ☐ 4 points ☐ Single

- monotonically decreasing
- monotonically increasing

- neither decreasing nor increasing ✓

(6) **Q3****CLOZE**

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\boxed{a}}{\boxed{b}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us consider the following function

$$f(x) = \log \left(\frac{-x}{x^2 + 1} \right).$$

The function $f(x)$ is not defined on the whole real line \mathbb{R} . Choose all the points that are **not** in the natural domain of $f(x)$.

MULTI

4 points

Single

- -2 (−100%)
- -1 (−100%)
- $-\frac{1}{2}$ (−100%)
- 0 ✓
- $\frac{1}{2}$ ✓
- 1 ✓
- 2 ✓

Choose all asymptotes of $f(x)$.

MULTI

4 points

Single

- $y = -1$ (−100%)
- $y = -\frac{1}{2}$ (−100%)
- $y = 0$ (−100%)
- $y = \frac{1}{2}$ (−100%)
- $y = 2$ (−100%)
- $x = -2$ (−100%)
- $x = -1$ (−100%)
- $x = -\frac{1}{2}$ (−100%)
- $x = 0$ ✓
- $x = \frac{1}{2}$ (−100%)
- $x = 1$ (−100%)
- $x = 2$ (−100%)
- $y = -x$ (−100%)
- $y = x$ (−100%)

One has

$$f'(-3) = \frac{\boxed{a}}{\boxed{b}}.$$

\boxed{a} :

4 points

4 ✓

\boxed{b} :

4 points

15 ✓

The function $f(x)$ has \boxed{c} stationary point(s) in the domain

\boxed{c} :

4 points

1 ✓

Choose the behaviour of $f(x)$ in the interval $(-4, -2)$.

4 points

- monotonically decreasing
- monotonically increasing ✓
- neither decreasing nor increasing

(7) Q4

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\boxed{a}}{\boxed{b}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us calculate the following integral.

$$\int_0^\pi x^2 \sin x dx.$$

By noting that we can find easily a primitive of $\sin(x)$, we can apply integration by parts. Fill in the blanks.

$$\int_0^\pi x^2 \sin x dx = \boxed{a} \pi - \int_0^\pi \boxed{b} dx.$$

Choose correct functions.

\boxed{a} :

3 points

- $x \sin(x)$

- $-x \cos(x)$
- $x^3 \cos(x)$
- $-x^2 \cos(x)$ ✓
- $-2x \cos(x)$
- $\sin(x)$
- $x \cos(x^2)$
- $2x \sin(x)$

:

- $x \sin(x)$
- $-x \cos(x)$
- $x^3 \cos(x)$
- $-x^2 \cos(x)$
- $-2x \cos(x)$ ✓
- $\sin(x)$
- $x \cos(x^2)$
- $2x \sin(x)$

By continuing the calculation, we obtain

$$\int_0^\pi x^2 \sin x dx = \boxed{\text{d}} + \boxed{\text{e}}\pi + \boxed{\text{f}}\pi^2.$$

:

✓

:

✓

:

✓

(8) **Q4**

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\boxed{\text{a}}}{\boxed{\text{b}}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Let us calculate the following integral.

$$\int_0^{\frac{\pi}{2}} x^2 \sin x dx.$$

By noting that we can find easily a primitive of $\sin(x)$, we can apply integration by parts. Fill in the blanks.

$$\int_0^{\frac{\pi}{2}} x^2 \sin x dx. = \boxed{a} \Big|_0^{\frac{\pi}{2}} - \int_0^{\frac{\pi}{2}} \boxed{b} dx.$$

Choose correct functions.

a:

MULTI

6 points

Single

- $x \sin(x)$
- $-x \cos(x)$
- $x^3 \cos(x)$
- $-x^2 \cos(x)$ ✓
- $-2x \cos(x)$
- $\sin(x)$
- $x \cos(x^2)$
- $2x \sin(x)$

b:

MULTI

6 points

Single

- $x \sin(x)$
- $-x \cos(x)$
- $x^3 \cos(x)$
- $-x^2 \cos(x)$
- $-2x \cos(x)$ ✓
- $\sin(x)$
- $x \cos(x^2)$
- $2x \sin(x)$

By continuing the calculation, we obtain

$$\int_0^{\frac{\pi}{2}} x^2 \sin x dx. = \boxed{d} + \boxed{e} \pi + \boxed{f} \pi^2.$$

d:

NUMERICAL

4 points

-2 ✓

e:

NUMERICAL

4 points

1 ✓

f:

NUMERICAL	4 points
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0 ✓	
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(9) Q5

CLOZE	0.10 penalty
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If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\boxed{a}}{\boxed{b}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Choose the general solution of the following differential equation.

$$y'(x) = 2 \exp(y(x)) \sin(x^2)x.$$

MULTI	2 points	Single
-------	----------	--------

- $y(x) = \exp(\cos(x^2)) + C$
- $y(x) = \log(\cos(x^2)) + C$
- $y(x) = \exp(-\cos(x^2)) + C$
- $y(x) = -\log(\cos(x^2)) + C$ ✓
- $y(x) = \exp(-\cos(x^2)) + C$
- $y(x) = -\log(\sin(x^2)) + C$
- $y(x) = -\log(\sin(x^2) + C)$
- $y(x) = \exp(-\sin(x^2)) + C$
- $y(x) = -\log(\sin(x^2)) + C$

Determine $C = \boxed{a}$ with the initial condition $y(0) = 0$

\boxed{a} :

NUMERICAL	2 points
-----------	----------

0 ✓	
-----	--

Choose the general solution of the following differential equation.

$$y''(x) + 5y'(x) + 4y(x) = 0.$$

MULTI	2 points	Single
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- $y(x) = C_1 \exp(2x) + C_2 \exp(-2x)$
- $y(x) = C_1 \exp(-x) + C_2 \exp(4x)$
- $y(x) = C_1 \exp(x) + C_2 \exp(-4x)$
- $y(x) = C_1 \exp(-x) + C_2 \exp(-4x)$ ✓
- $y(x) = C_1 \sin(-4x) + C_2 \cos(x)$
- $y(x) = C_1 \sin(-2x) + C_2 \cos(2x)$
- $y(x) = C_1 \sin(2x) + C_2 \cos(-2x)$
- $y(x) = C_1 \sin(x) + C_2 \cos(4x)$

Find a solution $y(x)$ such that $y(0) = 3$ and $y'(0) = 0$. $C_1 =$, $C_2 =$.

:

NUMERICAL

2 points

4 ✓

:

NUMERICAL

2 points

-1 ✓

For these values of C_1, C_2 , find a value $A =$ such that $\lim_{x \rightarrow \infty} y(x)/\exp(Ax) = 4$.

:

NUMERICAL

2 points

-1 ✓

(10) Q5

CLOZE

0.10 penalty

If not specified otherwise, fill in the blanks with **integers (possibly 0 or negative)**. A fraction should be **reduced** (for example, $\frac{1}{2}$ is accepted but not $\frac{2}{4}$), and if it is negative and the answer boxes (such as $\frac{\text{a}}{\text{b}}$) have ambiguity, the negative sign should be put on the numerator (for example $\frac{-1}{2}$ is accepted but $\frac{1}{-2}$ is not). $\log x = \log_e x$, not $\log_{10} x$.

Choose the general solution of the following differential equation.

$$y'(x) = 2 \exp(y(x)) \sin(x^2)x.$$

MULTI

2 points

Single

- $y(x) = \exp(\cos(x^2)) + C$
- $y(x) = \log(\cos(x^2)) + C$
- $y(x) = \exp(-\cos(x^2)) + C$
- $y(x) = -\log(\cos(x^2) + C)$ ✓
- $y(x) = \exp(-\cos(x^2)) + C$
- $y(x) = -\log(\sin(x^2)) + C$
- $y(x) = -\log(\sin(x^2) + C)$
- $y(x) = \exp(-\sin(x^2)) + C$
- $y(x) = -\log(\sin(x^2)) + C$

Determine $C =$ with the initial condition $y(\sqrt{\frac{\pi}{2}}) = 0$

:

NUMERICAL

2 points

1 ✓

Choose the general solution of the following differential equation.

$$y''(x) - 5y'(x) + 4y(x) = 0.$$

MULTI

2 points

Single

- $y(x) = C_1 \exp(2x) + C_2 \exp(-2x)$
- $y(x) = C_1 \exp(-x) + C_2 \exp(4x)$
- $y(x) = C_1 \exp(x) + C_2 \exp(4x)$ ✓
- $y(x) = C_1 \exp(-x) + C_2 \exp(-4x)$
- $y(x) = C_1 \sin(-4x) + C_2 \cos(x)$
- $y(x) = C_1 \sin(-2x) + C_2 \cos(2x)$
- $y(x) = C_1 \sin(2x) + C_2 \cos(-2x)$
- $y(x) = C_1 \sin(x) + C_2 \cos(4x)$

Find a solution $y(x)$ such that $y(0) = 6$ and $y'(0) = 0$. $C_1 =$

, $C_2 =$.

.

NUMERICAL

2 points

8 ✓

.

NUMERICAL

2 points

-2 ✓

For these values of C_1, C_2 , find a value $A =$ such that $\lim_{x \rightarrow \infty} y(x) / \exp(Ax) = -2$.

.

NUMERICAL

2 points

4 ✓

Total of marks: 258