

Proposed solution to problem O689

Prove that $5/2$ is the minimum positive value of the constant k such that

$$\sqrt{\frac{b+c}{ka+b+c}} + \sqrt{\frac{c+a}{kb+c+a}} + \sqrt{\frac{a+b}{kc+a+b}} \geq 3\sqrt{\frac{2}{k+2}}$$

holds for any nonnegative real numbers a, b, c with $a + b + c > 0$.