



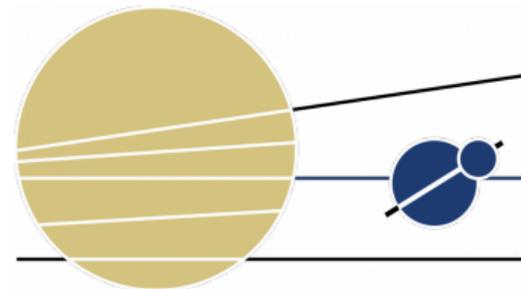
# Comparison of Stratified and Effective Rheological Models For Icy Worlds

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Lunar and Planetary Laboratory

## Research questions

- Moons and planets modeled after homogeneous laboratory-based rheologies
- Two layered and homogeneous models used to predict core-mantle mechanical decoupling from measured librations
- Mimicking the dissipative behavior of a stratified body with a complex homogeneous laboratory-based rheological model

## Contents

- Andrade rheology in the time domain: Enceladus
- Librations of a body with a deformable mantle and a fluid core: Enceladus
- Sundberg-Cooper rheology vs stratified rheology: TRAPPIST-1e planet

## General rheology

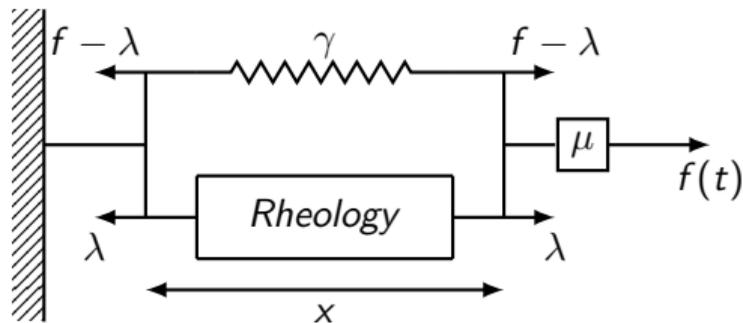


Figure: General oscillator. The rheology can be replaced by the rheologies below, for example.

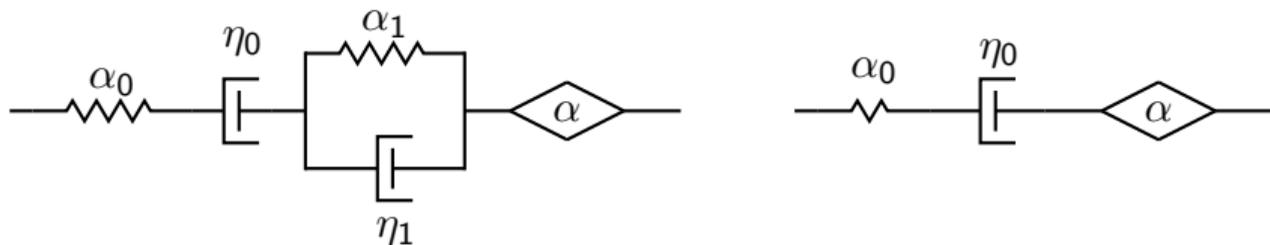
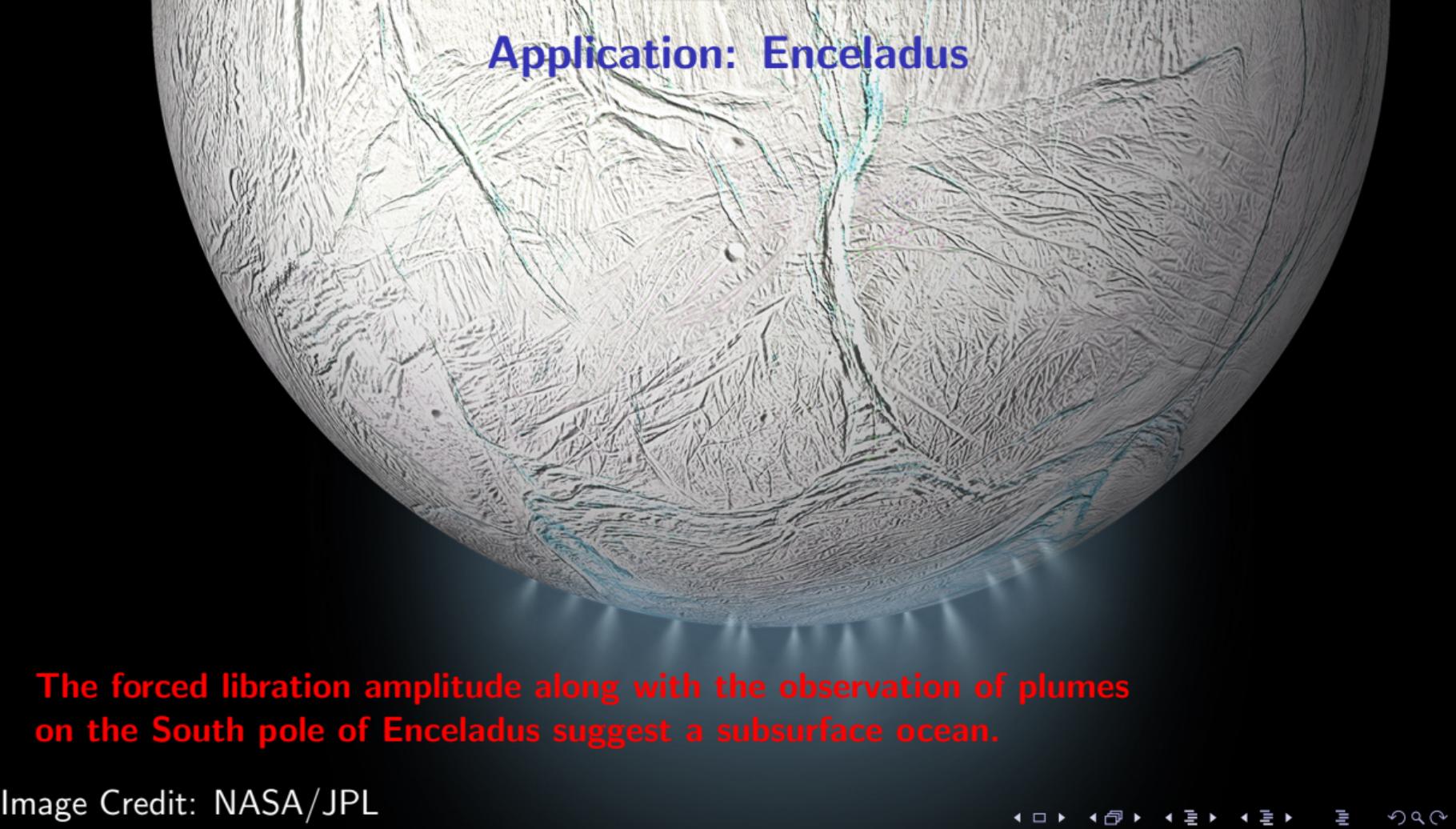


Figure: The Sundberg-Cooper model (left) and the Andrade model (right)

## Application: Enceladus



**The forced libration amplitude along with the observation of plumes on the South pole of Enceladus suggest a subsurface ocean.**

# Observed vs modeled librations with Andrade rheology

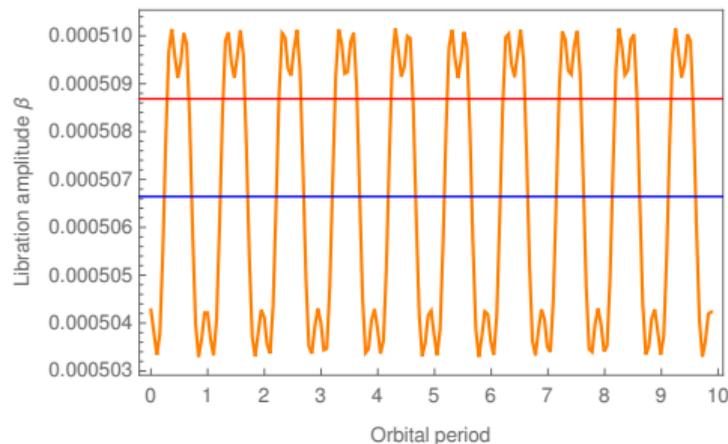


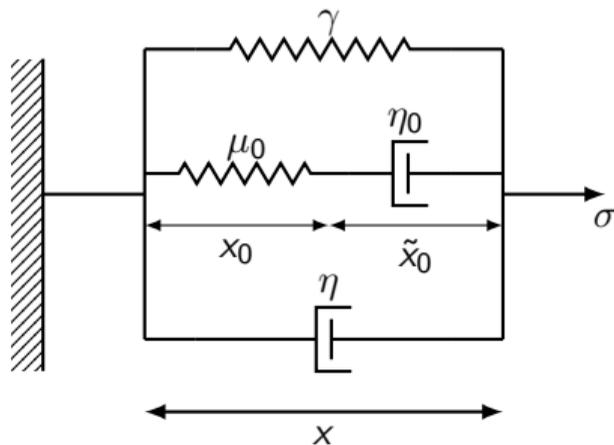
Figure: Andrade rheology: Libration of Enceladus

Modeled libration  $\sim 0.000508$  rad  
vs observed  $0.0021$  rad (Thomas et al. 2016) or  $0.0027$  rad (Nadezhdina et al. 2016)

- Can be explained by assuming core libration of  $\sim 0.6\%$  of that of the shell

## Two layered body

- Can we reproduce observed librations of an ocean world with two layered model?
- Observed vs mantle vs Tisserand frame librations
- Forced libration amplitude as an argument for core-mantle mechanical decoupling



**Figure: Mantle rheology:** The damper  $\eta$  and the Maxwell element ( $\mu_0, \eta_0$ ) represent the effect of the macroscopic (spatial average) rheology of the mantle;  $x$ ,  $x_0$  and  $\tilde{x}_0$  denote strains and  $\sigma$  the stress

# Mantle vs Tisserand frame vs observed librations of Enceladus

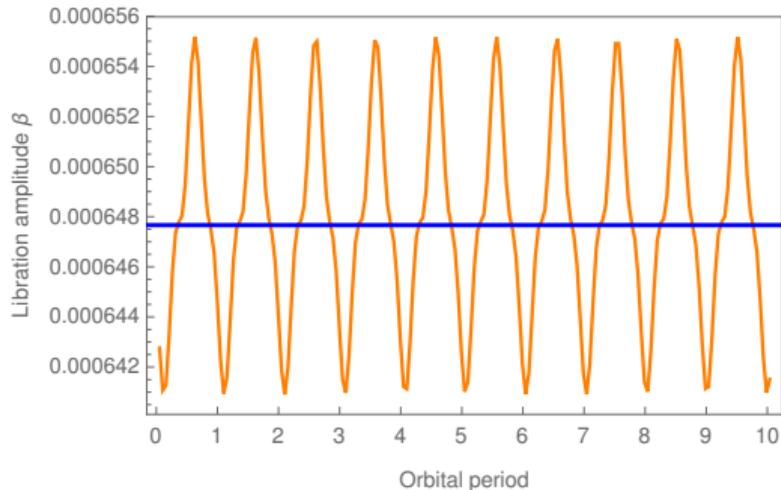
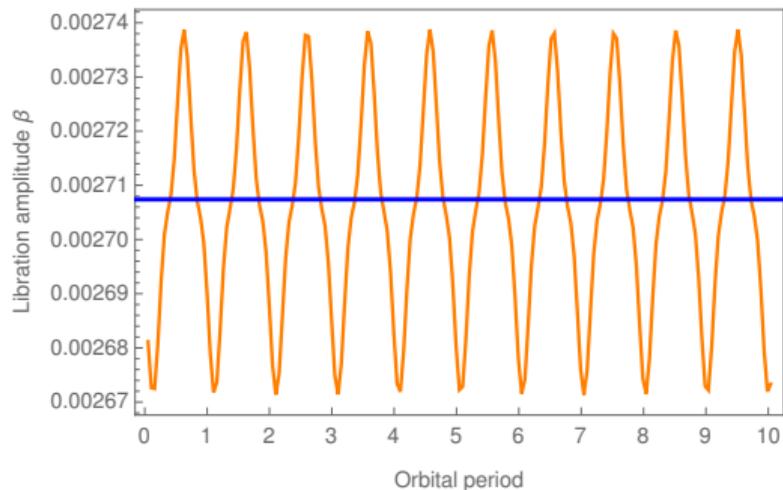


Figure: Libration amplitude comparison

Mantle  $\sim 0.00271$  rad vs Tisserand frame  $\sim 0.000648$  rad  
vs observed  $0.0021$  rad (Thomas et al. 2016) or  $0.0027$  rad (Nadezhdina et al. 2016)

# TRAPPIST-1e planet with an icy layer

- **Suggested internal structure**

Five layers: liquid core, two mantle layers, two ice layers

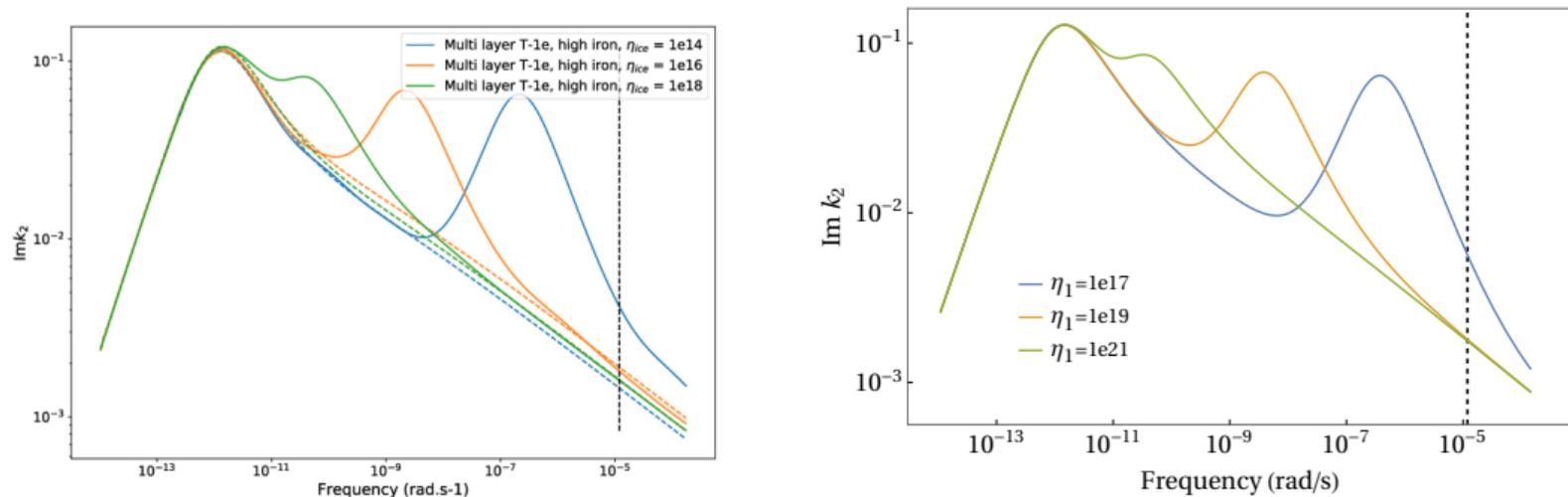
- **The effect of the icy crust**

Second peak in the tidal response at higher frequencies

- **Sundberg–Cooper rheology**

The homogeneous rheology mimics well multilayered dissipative behavior

# TRAPPIST-1e modeled with stratified vs homogeneous rheology



**Figure:** Frequency dependence of the dissipation.

The left figure is taken from Bolmont et al. (2020, Fig. 11) and was obtained with a stratified rheology. The right figure was obtained with a homogeneous Sundberg-Cooper rheology in Gevorgyan (2021, Fig. 4).

## Conclusions

- Laboratory-based homogeneous rheologies are important to model bodies with little observational data available
- Two layered rheology can be used to model librations of a body with a subsurface ocean
- Homogeneous rheology can be used to model dissipation of an icy body with no ocean

## References

- Gevorgyan, Y. *A & A* **650**, A141 (2021).
- Gevorgyan, Y. et al. *Icarus* **343**, 113610 (2020).