

# Applications of invariant manifolds in astrodynamics

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# Personal background

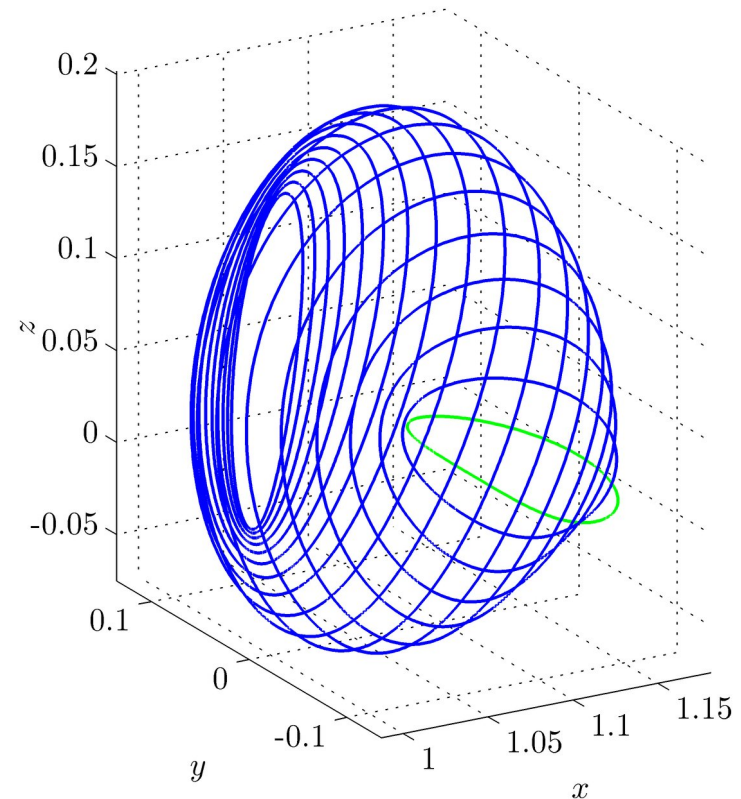
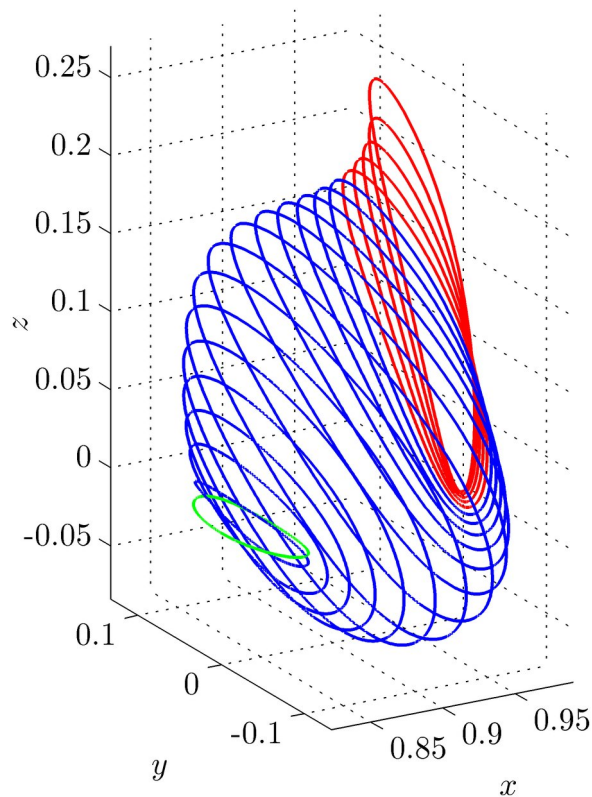
- B.S. in Aeronautical & Astronautical Engineering, 2007; Purdue University
- M.S. in Aeronautics & Astronautics, 2010; Purdue University  
(Advisor: Kathleen C. Howell)
- Ph.D. in Aerospace Engineering Sciences, *in progress*; University of Colorado Boulder  
(Advisor: Daniel J. Scheeres)
- AstroNet-II ESR; IEEC-UB (Scientists-in-charge: Gerard Gómez and Josep J. Masdemont)

Use natural dynamics to design efficient spacecraft trajectories satisfying mission objectives and constraints

# Invariant manifold tools

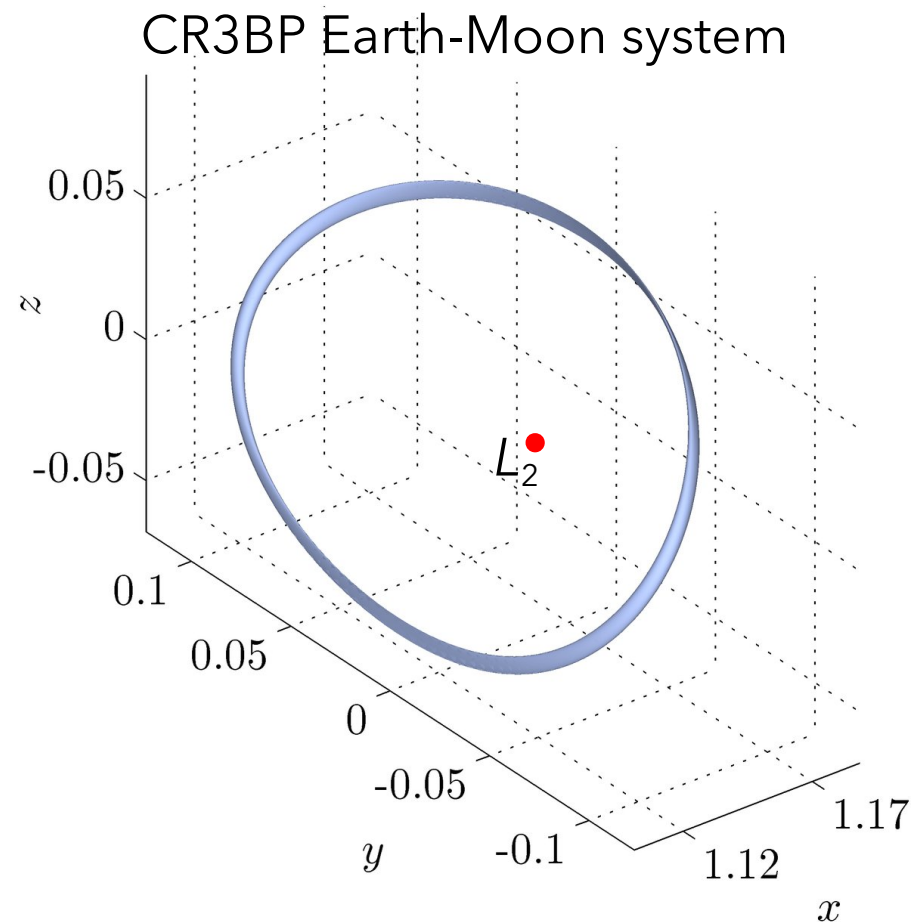
- Computation of periodic orbits and associated manifolds

CR3BP Earth-Moon system



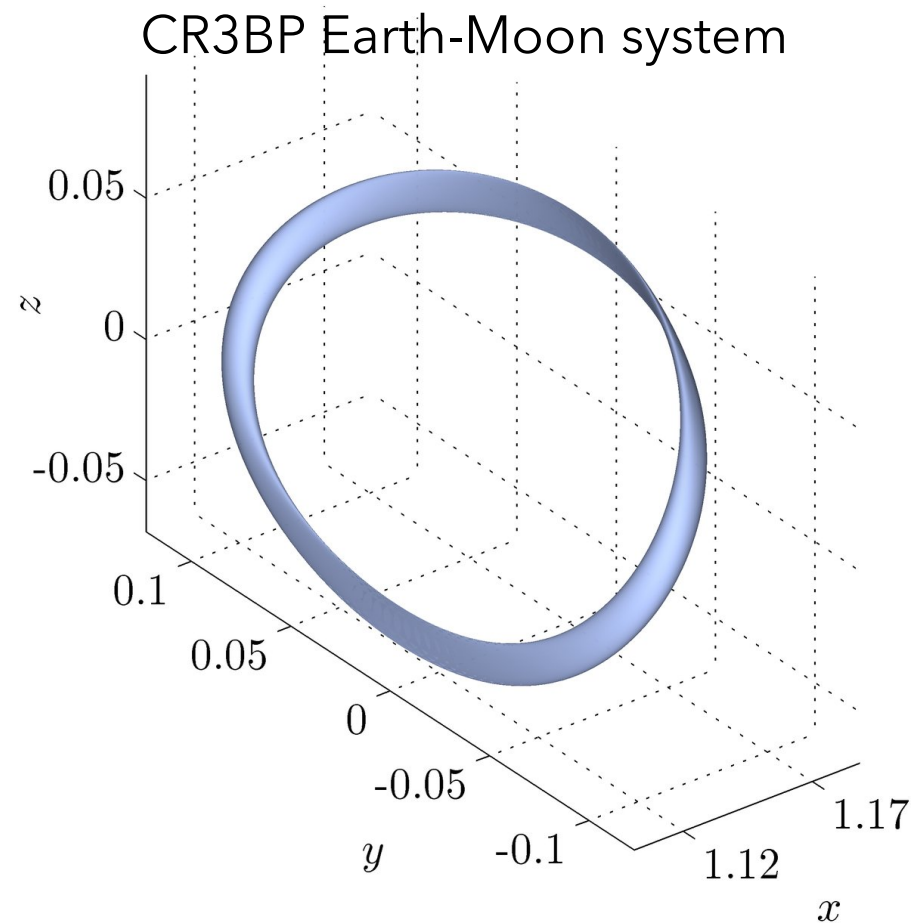
# Invariant manifold tools

- Computation of quasi-periodic orbits and associated manifolds



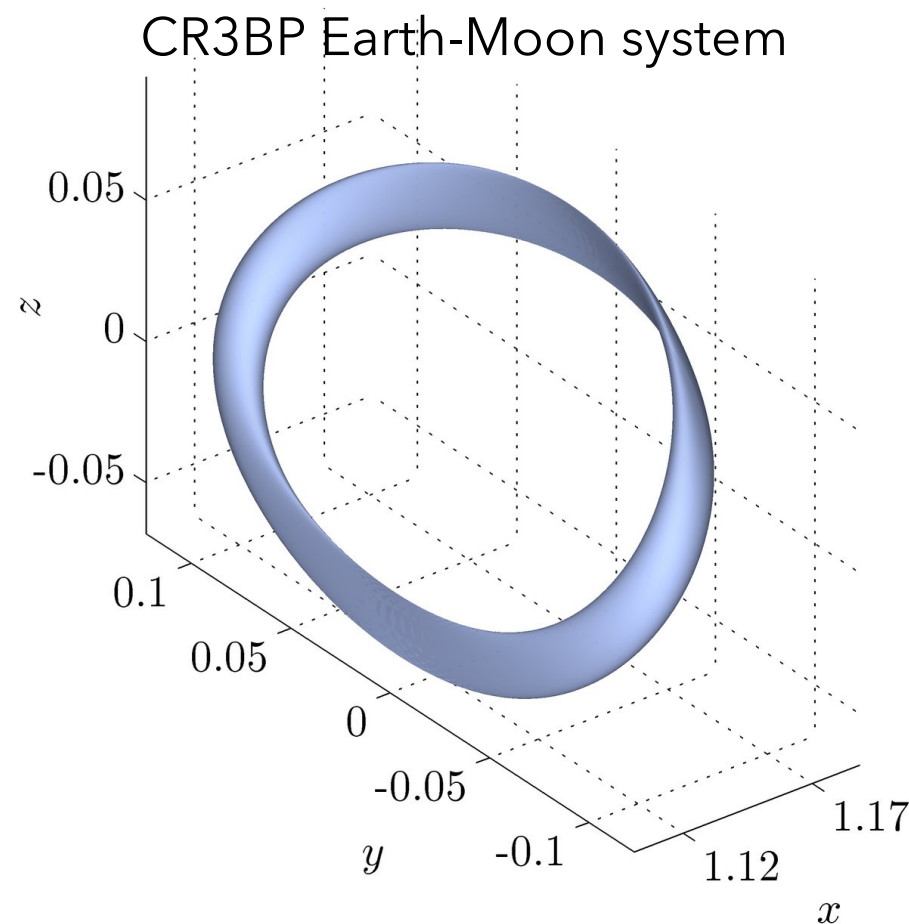
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- Computation of quasi-periodic orbits and associated manifolds



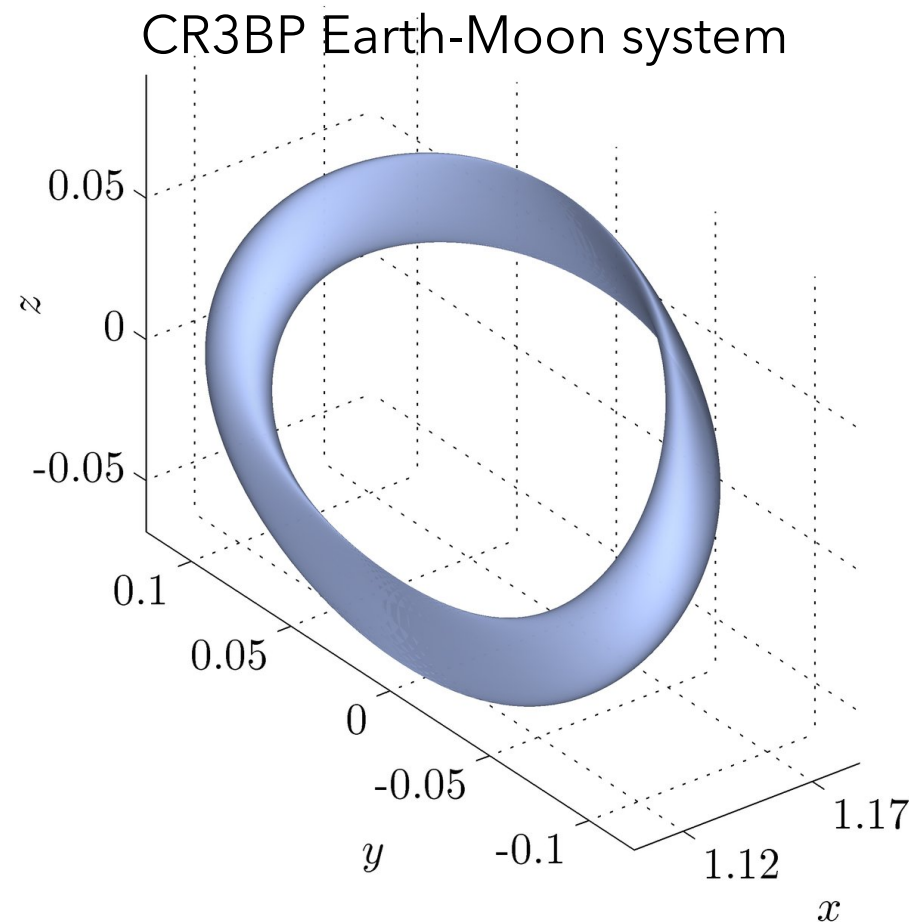
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- Computation of quasi-periodic orbits and associated manifolds



# Invariant manifold tools

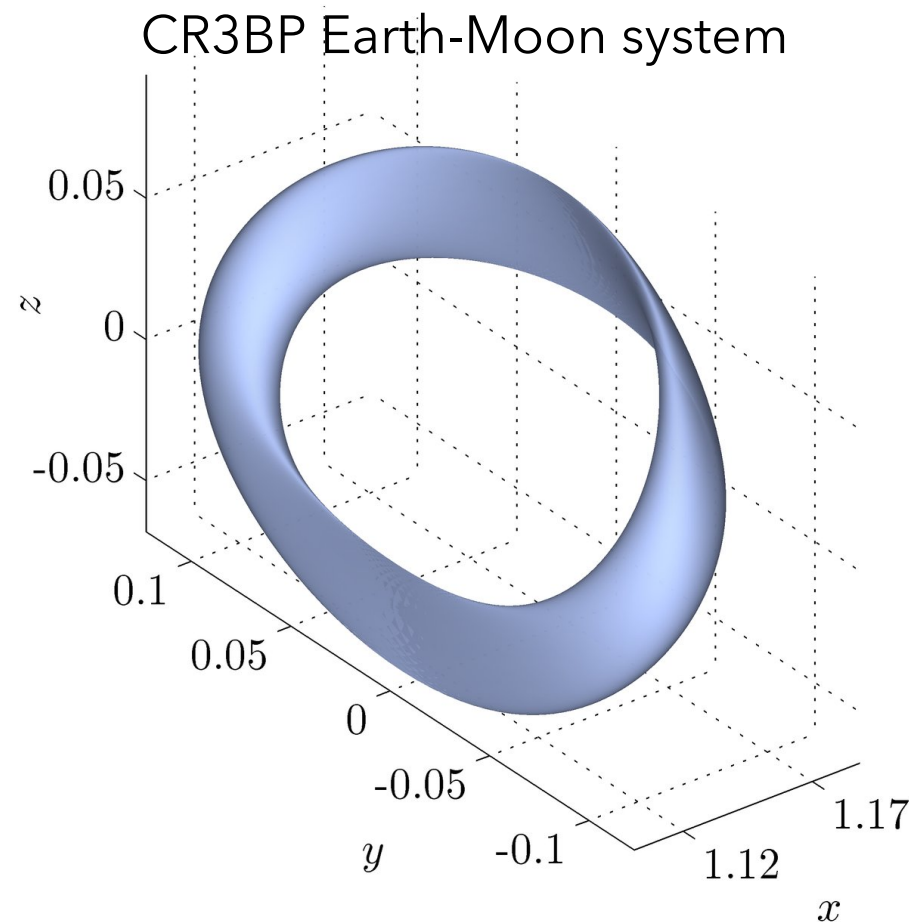
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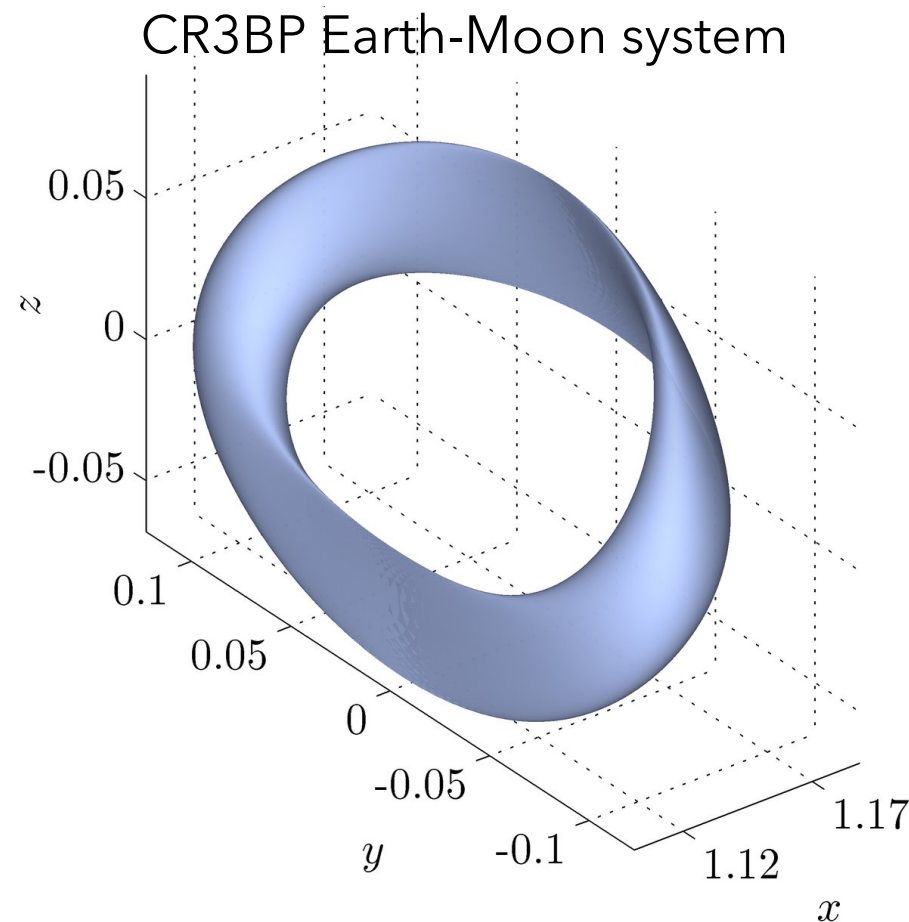
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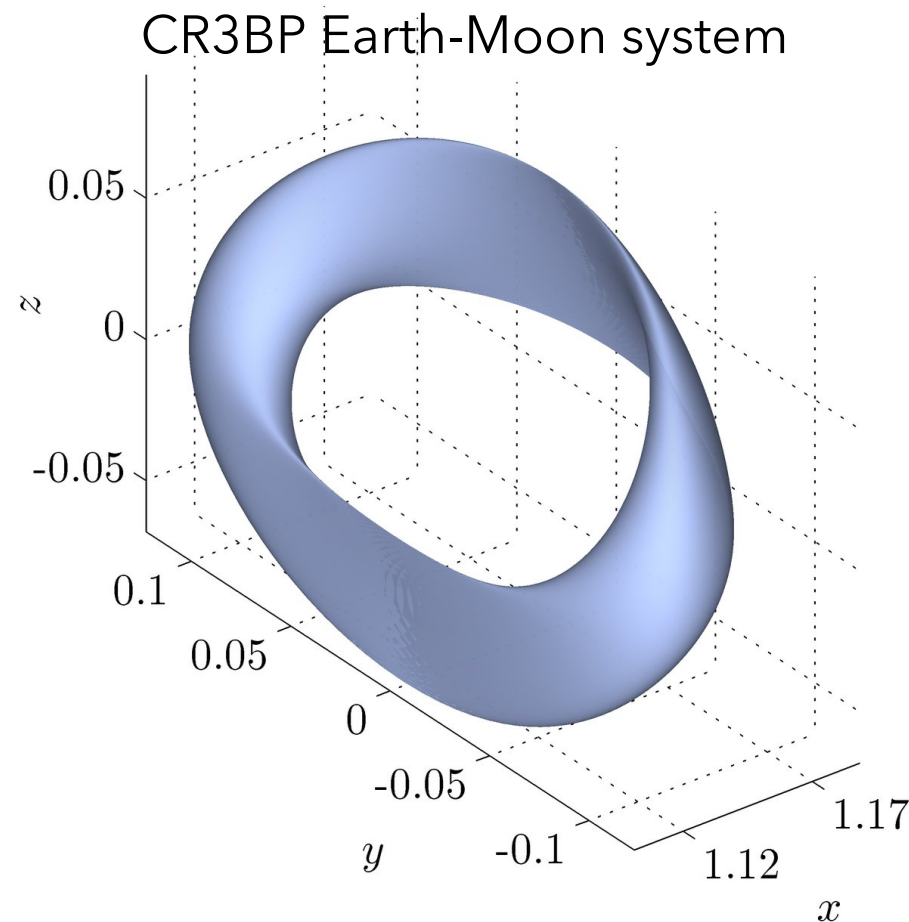
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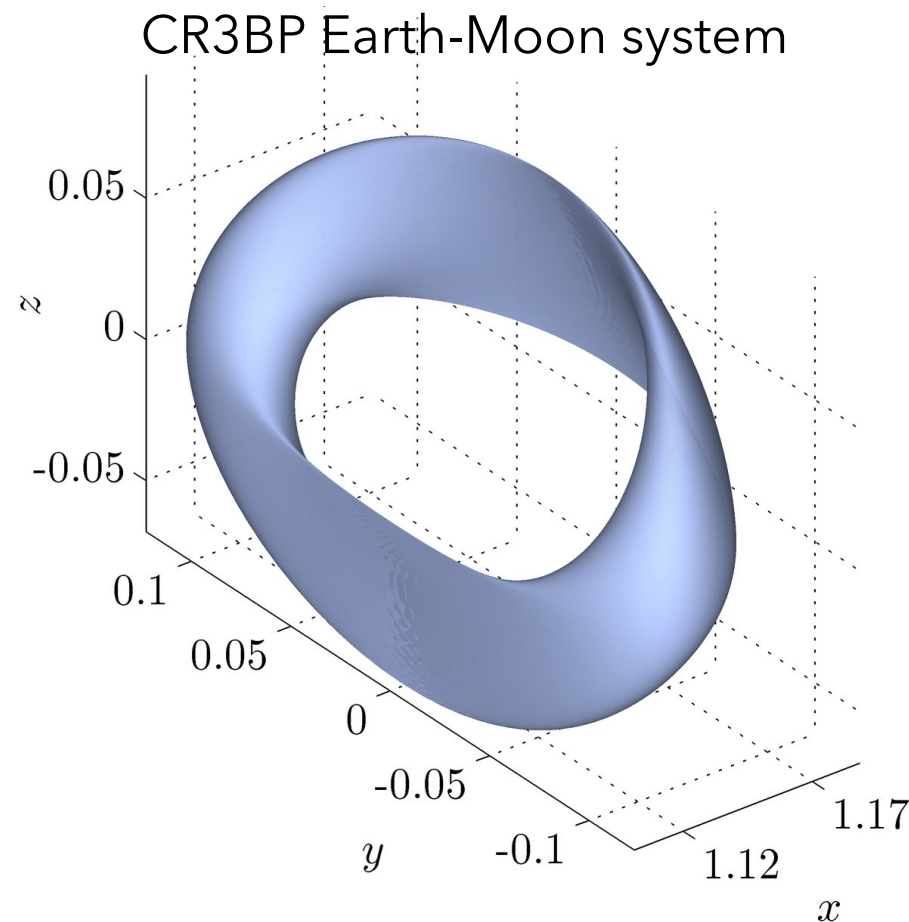
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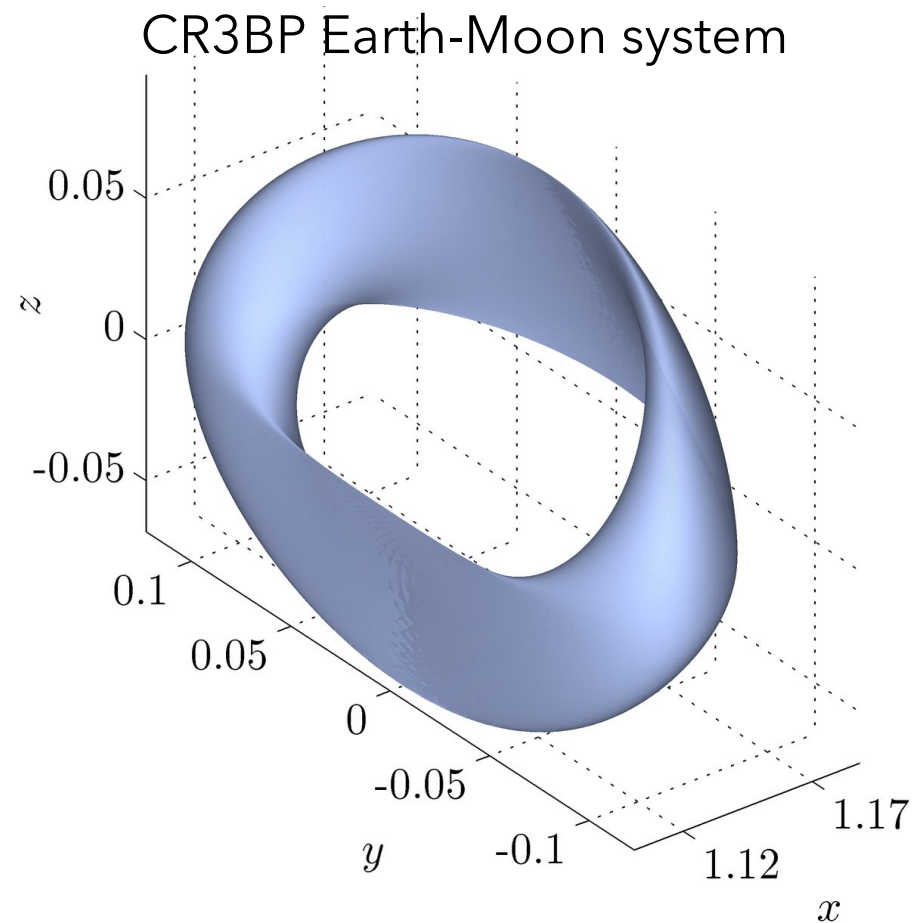
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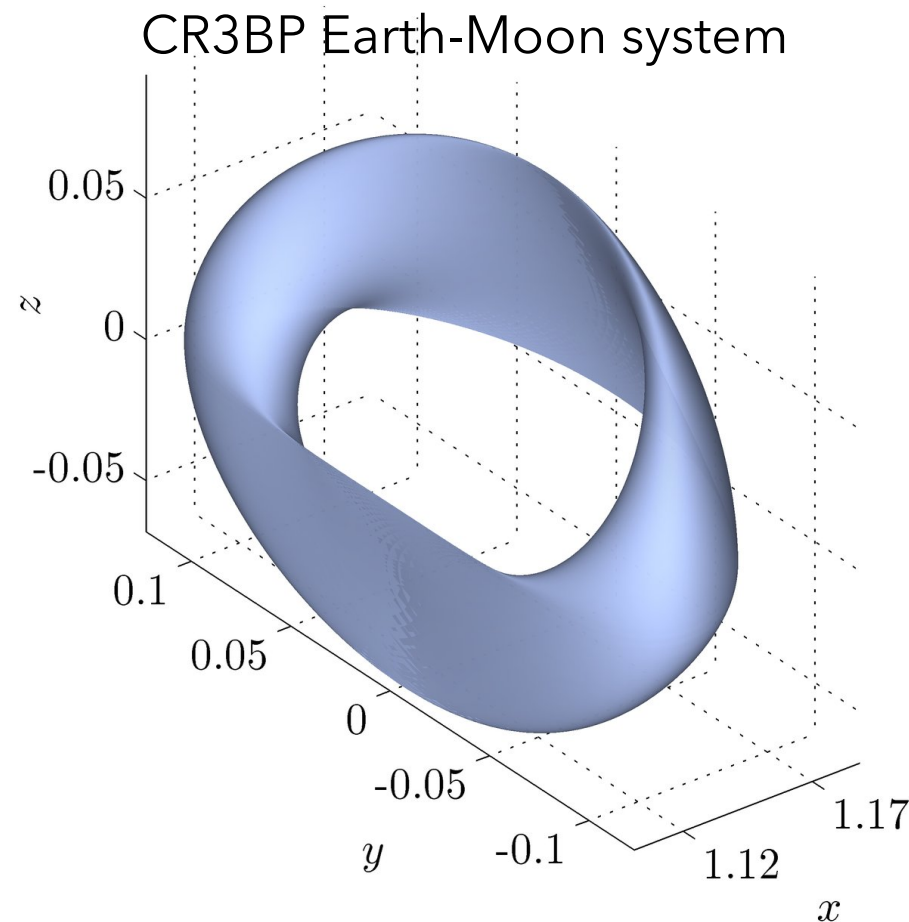
# Invariant manifold tools

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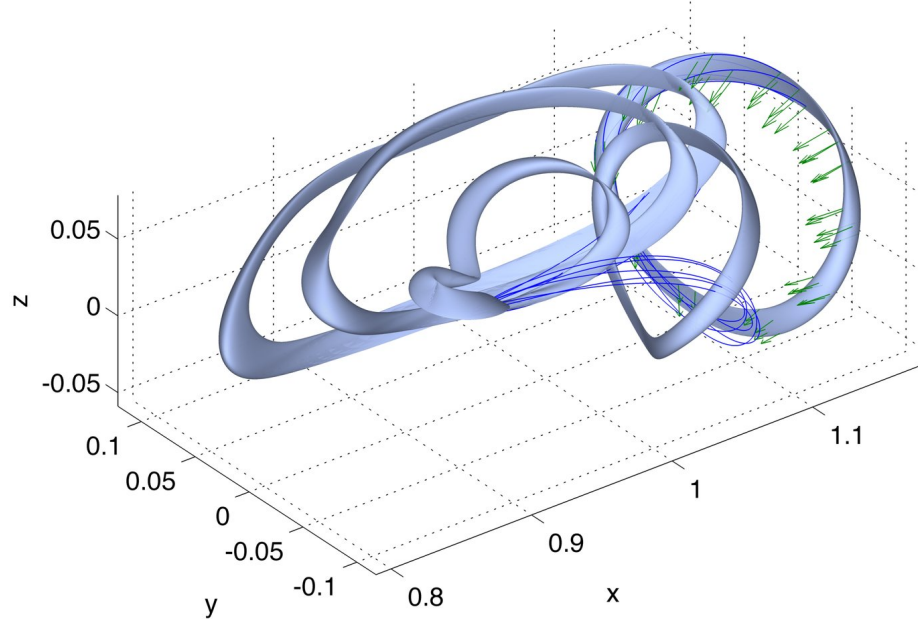


# Invariant manifold tools

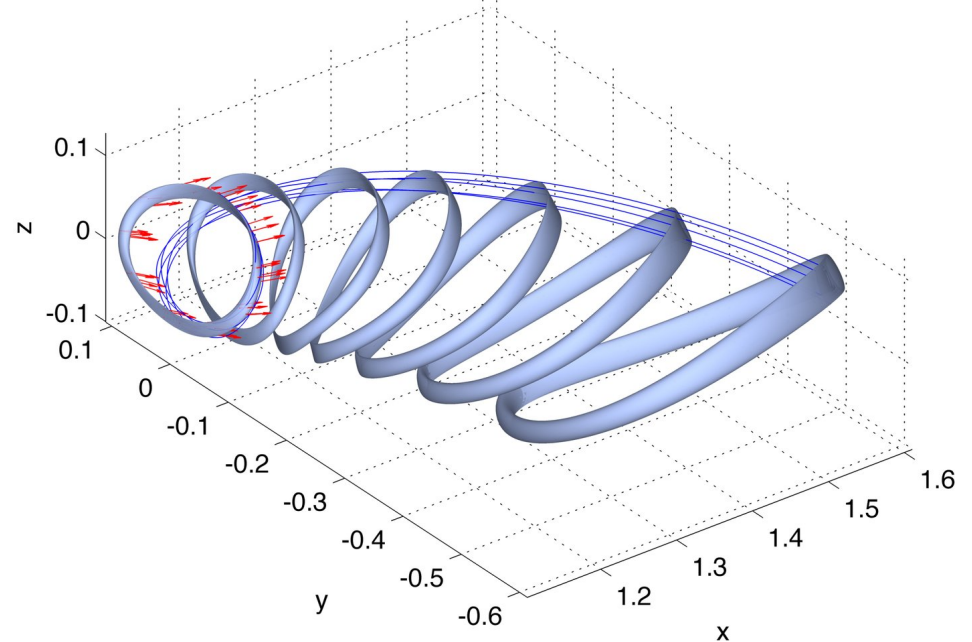
- Computation of quasi-periodic orbits and associated manifolds

CR3BP Earth-Moon system

Stable manifold

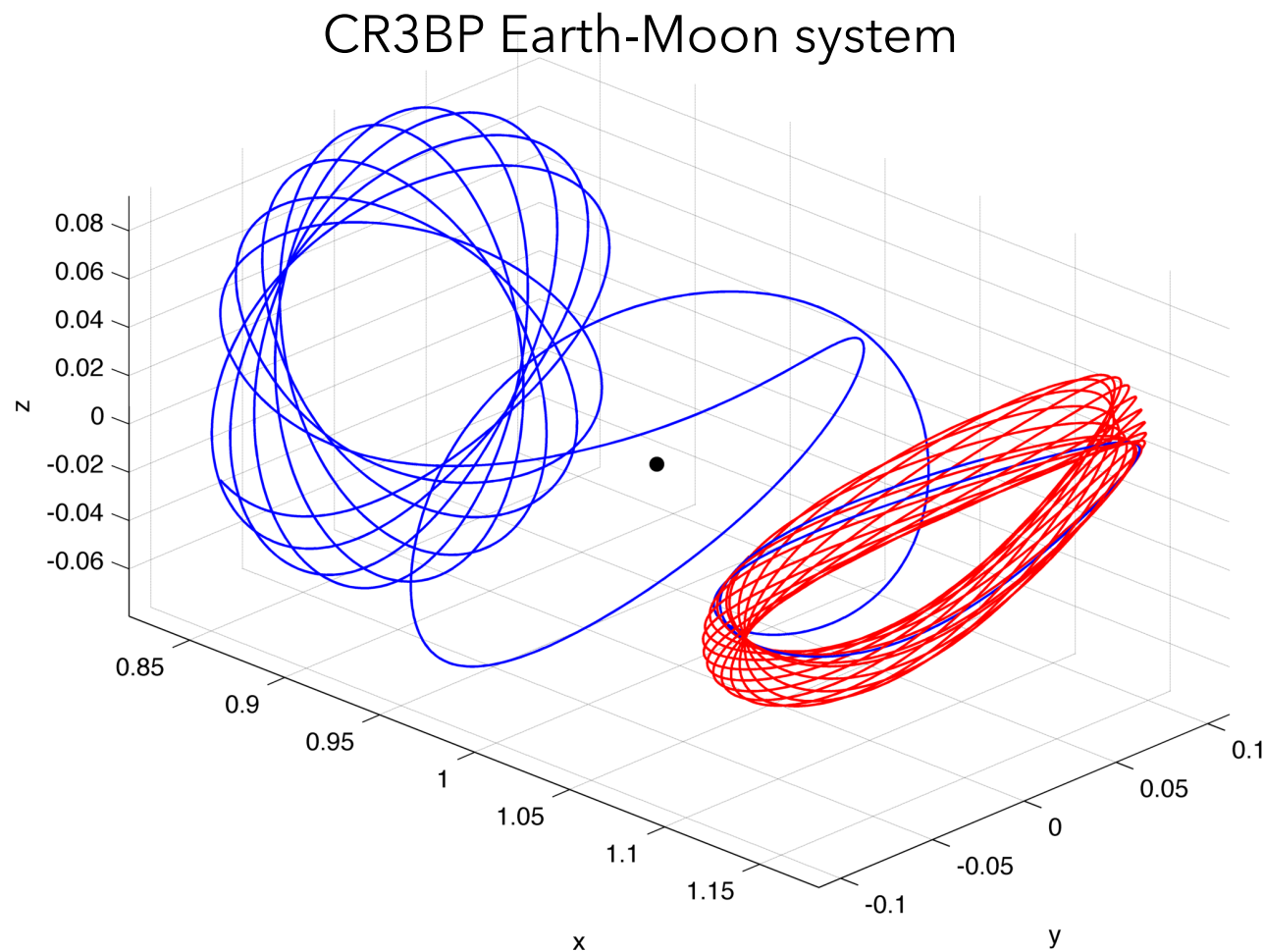


Unstable manifold



# Invariant manifold tools

- Locating connecting orbits between quasi-periodic solutions





# Application: Motion near binary asteroid

- ESA interest in binary asteroid mission:  
e.g., MarcoPolo-R sample return proposal
- Study dynamics in vicinity of binary asteroids by finding invariant solutions



(Antiope asteroid illustration, source: ESO)

# Application: End-of-life mission design

- Invariant manifolds show set of natural outcomes for spacecraft in libration point orbit
- Use as framework for designing end-of-life trajectories; potentially incorporate control such as solar sail