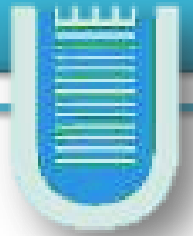


First AstroNet-II Training School  
University of Roma Tor Vergata

AstroNet-II Early Stage Researcher:

# Dissipative Effects on Attitude Dynamics

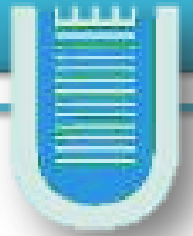
Marta Ceccaroni



# Backbackground

Bachelor & Master:

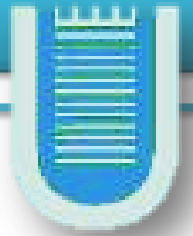
- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



# Backbackground

## Bachelor & Master:

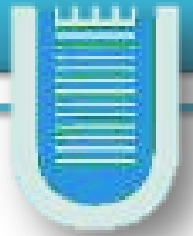
- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



# Backbackground

Bachelor & Master:

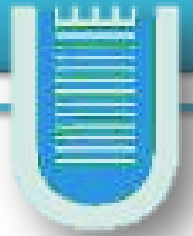
- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



# Backbackground

Bachelor & Master:

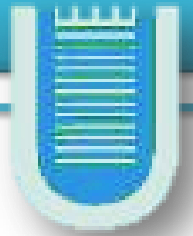
- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



# Backbackground

Bachelor & Master:

- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



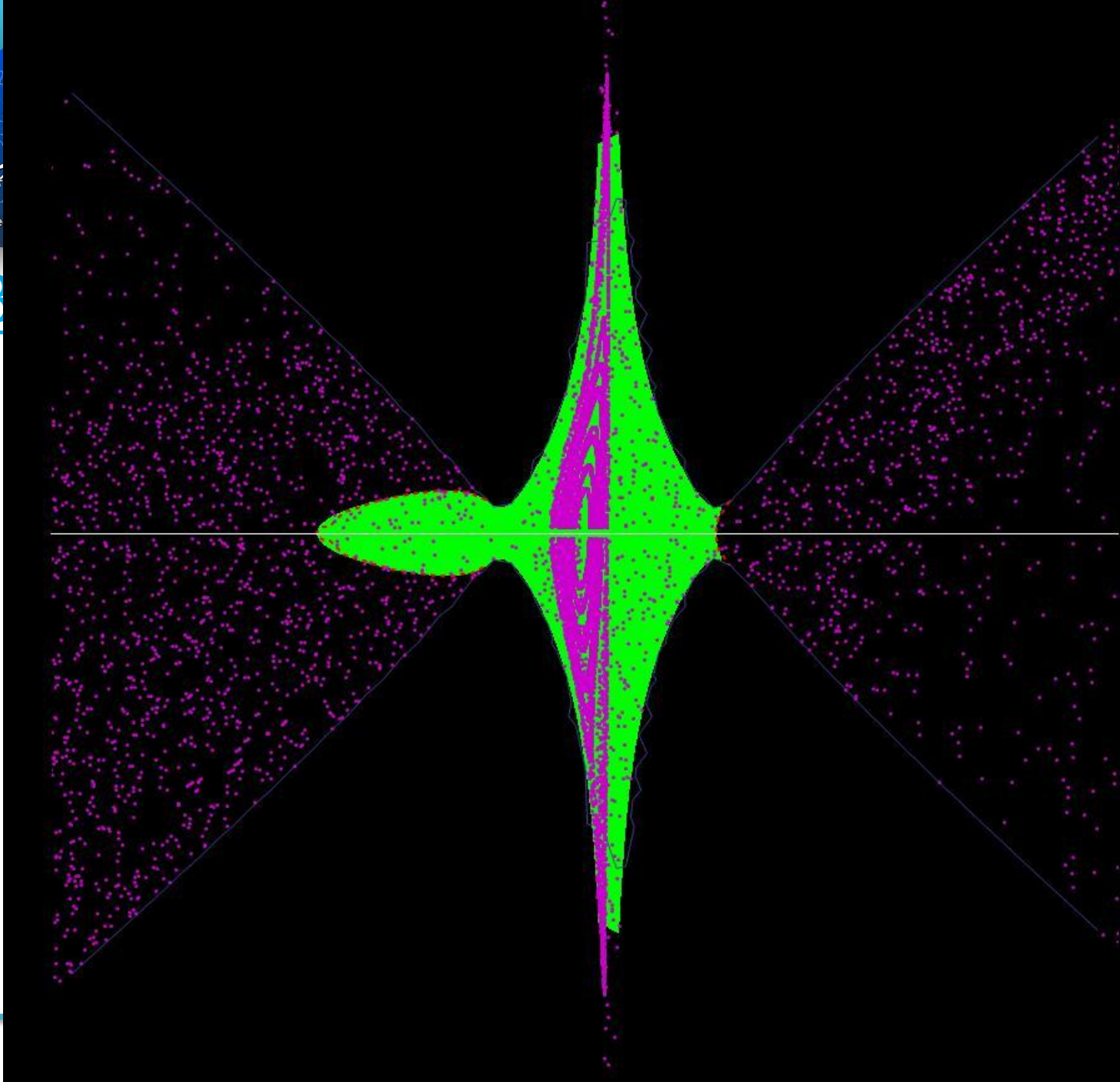
# Backbackground

Bachelor & Master:

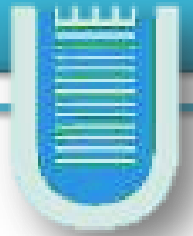
- University of Roma Tre, Rome
- Department of Mathematics
- Differential Equations and Functional Analysis
- Master Thesis: The Weak Stability Boundary



B  
B  
-  
-  
-  
-



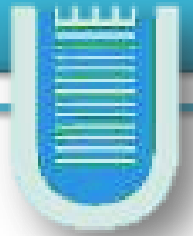




## Recent background

PhD:

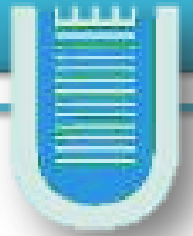
- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies



## Recent background

### PhD:

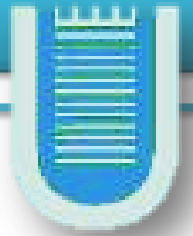
- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies



## Recent background

PhD:

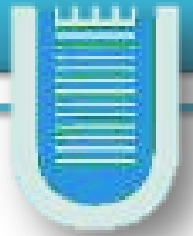
- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies



## Recent background

PhD:

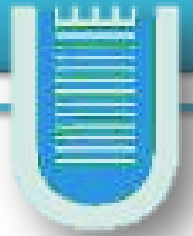
- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies



## Recent background

PhD:

- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies



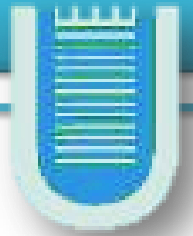
## Recent background

### PhD:

- Strathclyde University (prof. James Biggs)
- Advanced Space Concepts Laboratory
- PhD thesis: Natural and perturbed dynamics around Trojan bodies

### ESA ARIADNA STUDY:

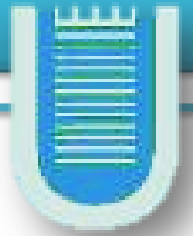
- Analytical perturbative theories of motion in highly inhomogeneous gravitational fields (Francesco Biscani)



## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

- \* new, general, analytical WSB theory  
=>estimation of the 'stable' zone around a Trojan
- \* INSIDE: Inhomogeneous CR2BP , analitic closed  
form perturbative theories in highly inhomogeneous gravitational fields  
=> frozen orbits
- \* OUTSIDE: Lagrangian CR4BP +Low thrust,  
=>artificial non-Keplerian orbits



## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

- \* new, general, analytical WSB theory  
=>estimation of the 'stable' zone around a Trojan
- \* INSIDE: Inhomogeneous CR2BP , analitic closed  
form perturbative theories in highly inhomogeneous gravitational fields  
=> frozen orbits
- \* OUTSIDE: Lagrangian CR4BP +Low thrust,  
=>artificial non-Keplerian orbits

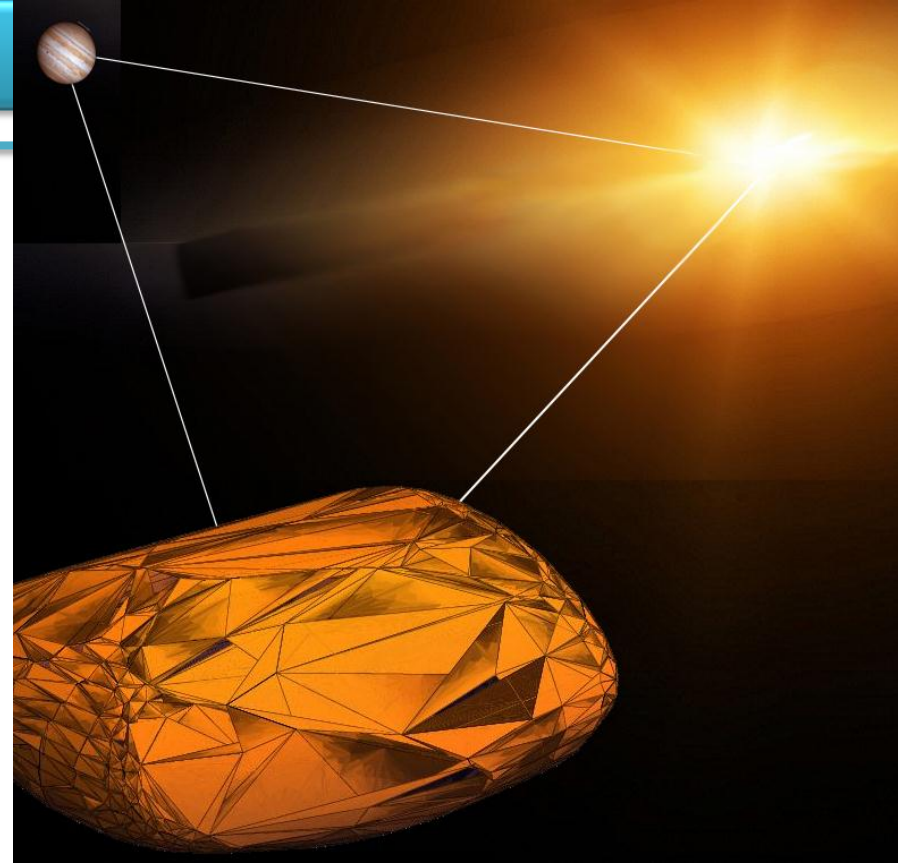


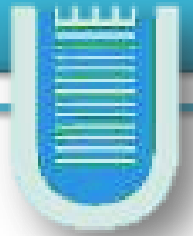


## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

- \* new, general, analytical WSB theory  
=> estimation of the 'stable' zone around a Trojan
- \* INSIDE: Inhomogeneous CR2BP, analytic closed  
form perturbative theories in highly inhomogeneous gravitational fields  
=> frozen orbits
- \* OUTSIDE: Lagrangian CR4BP + Low thrust,  
=> artificial non-Keplerian orbits





## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

\* new, general, analytical WSB theory

=>estimation of the 'stable' zone around a Trojan [1]

\* INSIDE: Inhomogeneous CR2BP, analitic closed

form perturbative theories in highly inhomogeneous gravitational fields

=> frozen orbits

\* OUTSIDE: Lagrangian CR4BP +Low thrust,

=>artificial non-Keplerian orbits

## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

\* new, general, analytical WSB theory

=> estimation of the 'stable' zone around a Trojan <sup>[1]</sup>

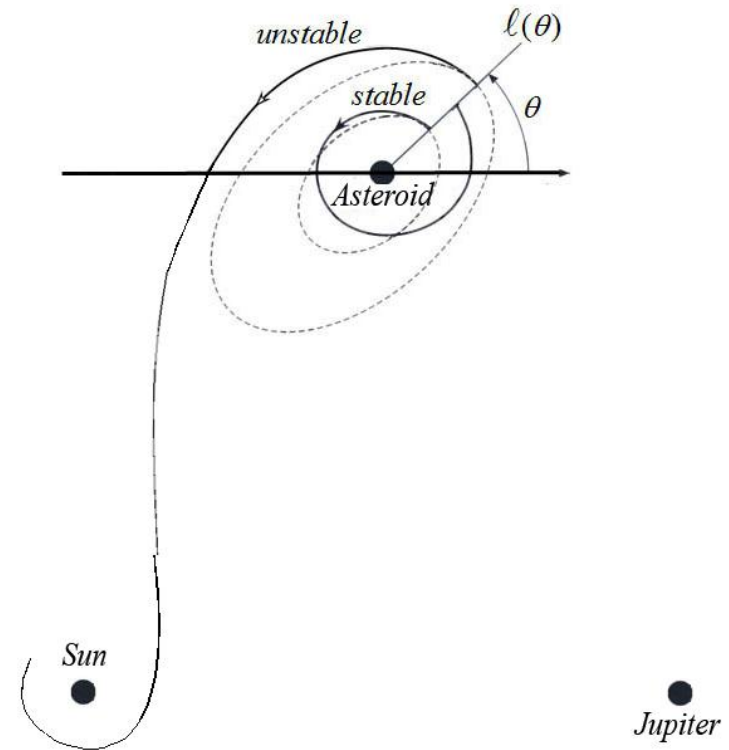
\* INSIDE: Inhomogeneous CR2BP, analytic closed

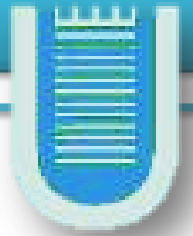
form perturbative theories in highly inhomogeneous gravitational fields

=> frozen orbits

\* OUTSIDE: Lagrangian CR4BP + Low thrust,

=> artificial non-Keplerian orbits





## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

\* new, general, analytical WSB theory

=>estimation of the 'stable' zone around a Trojan

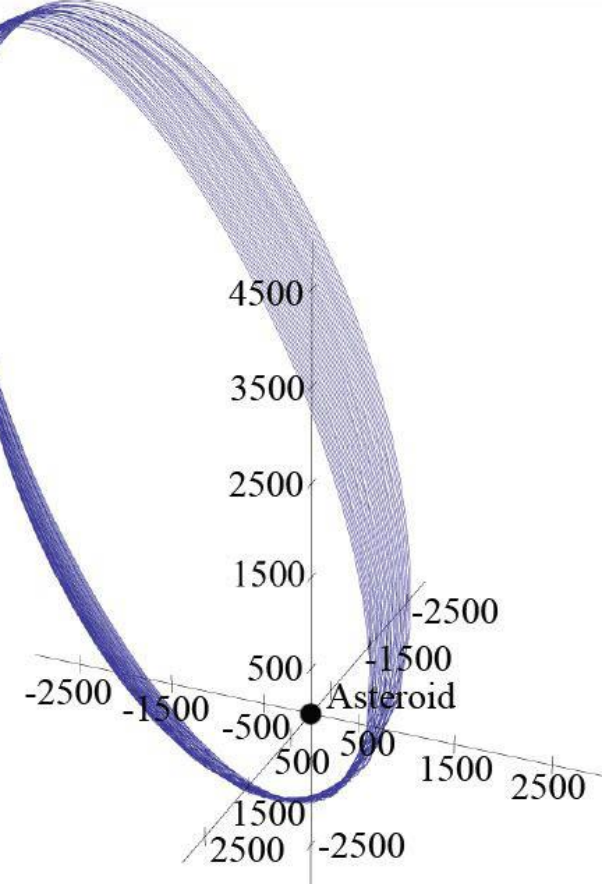
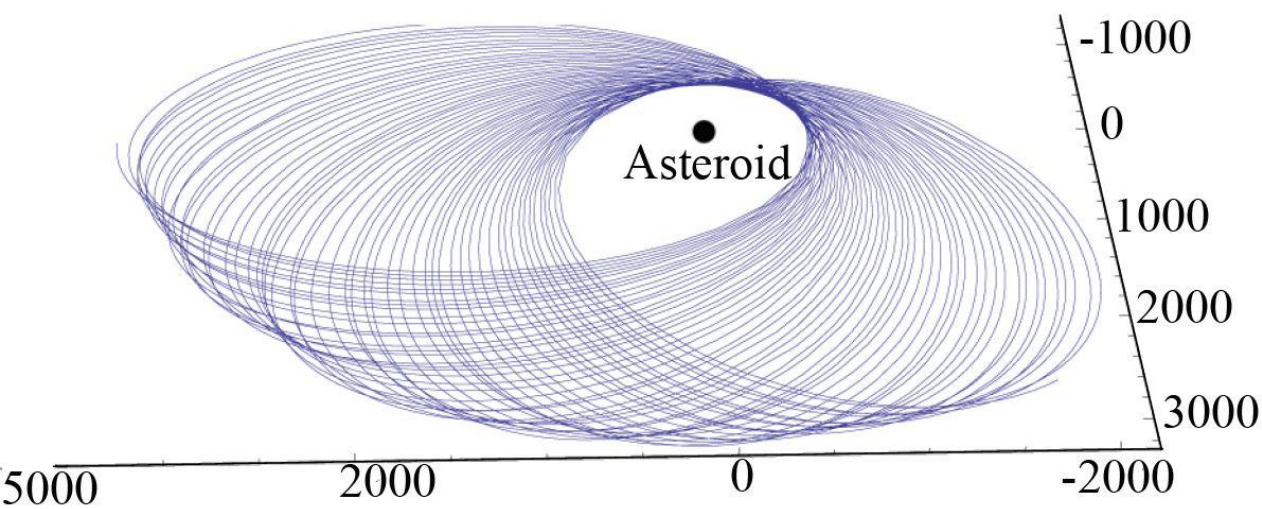
\* INSIDE: Inhomogeneous CR2BP, analitic closed

form perturbative theories in highly inhomogeneous gravitational fields

=> frozen orbits

\* OUTSIDE: Lagrangian CR4BP +Low thrust,

=>artificial non-Keplerian orbits



Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

\* new, general, analytical WSB theory

=>estimation of the 'stable' zone around a Trojan

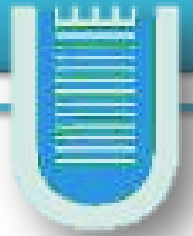
\* INSIDE: Inhomogeneous CR2BP , analitic closed

form perturbative theories in highly inhomogeneous gravitational fields

=> frozen orbits [2] [3]

\* OUTSIDE: Lagrangian CR4BP +Low thrust,

=>artificial non-Keplerian orbits



## Recent background

Three masses in Lagrangian configuration,  
(Sun-Jupiter-624Hektor-Spacecraft)

\* new, general, analytical WSB theory

=>estimation of the 'stable' zone around a Trojan

\* INSIDE: Inhomogeneous CR2BP, analitic closed

form perturbative theories in highly inhomogeneous gravitational fields

=> frozen orbits

\* OUTSIDE: Lagrangian CR4BP +Low thrust,

=>artificial non-Keplerian orbits [4]



# Recent background

a)

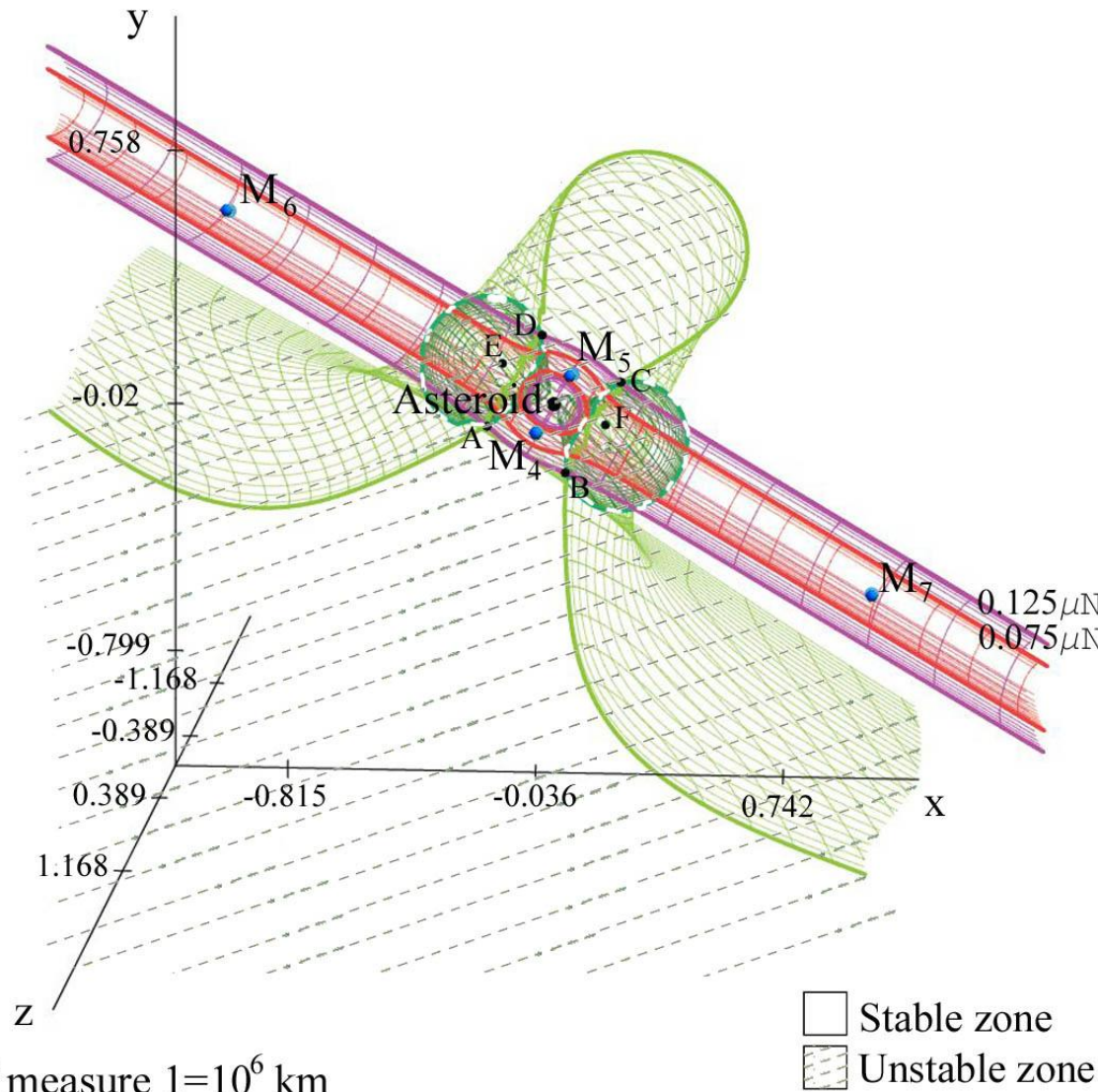
Three masses in Lagrangian co-orbitals  
(Sun-Jupiter-624Hektor-Space)

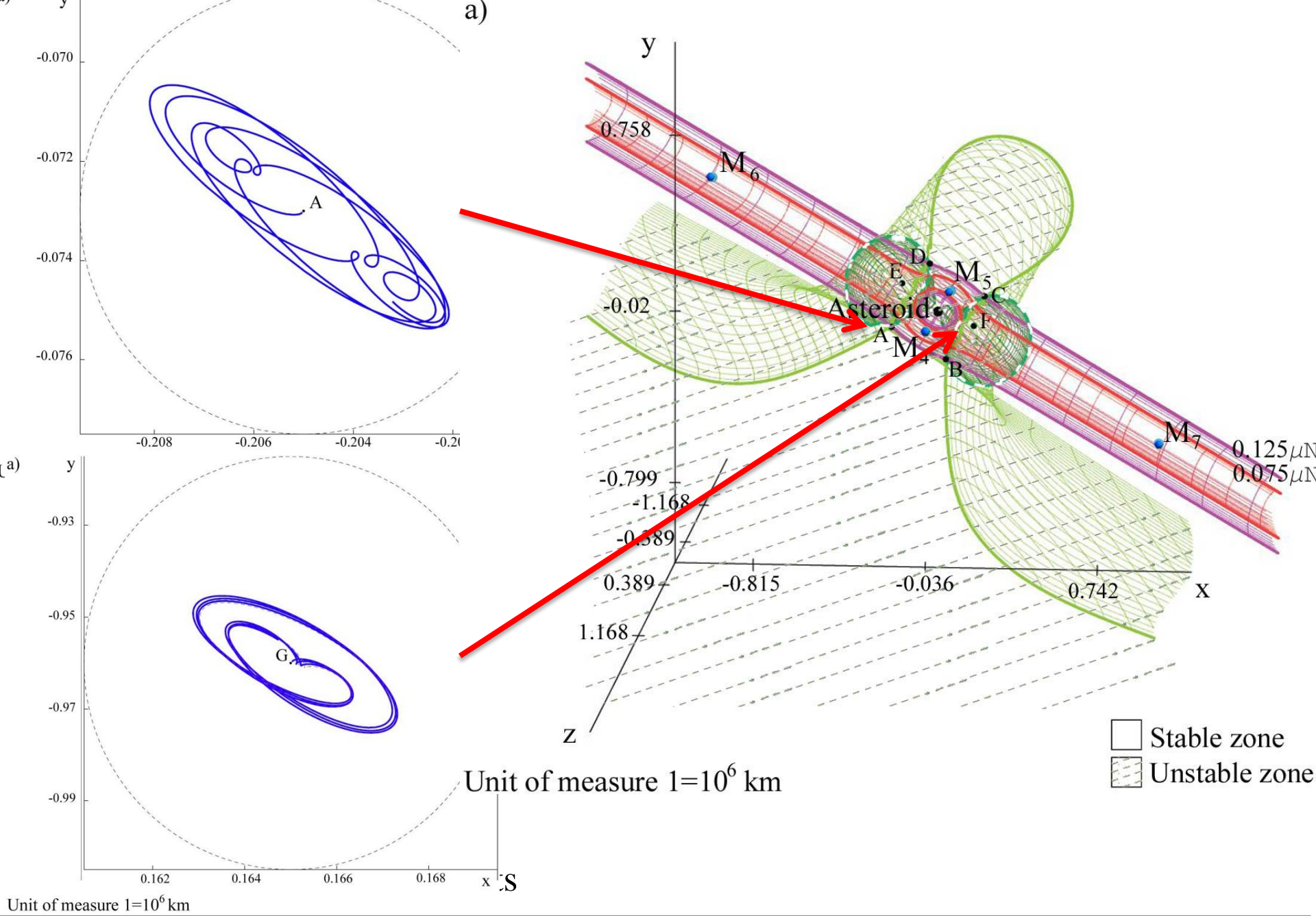
\* new, general, analytical WSE  
=> estimation of the 'stable' zones

\* INSIDE: Inhomogeneous Classical  
form perturbative theories in  
=> frozen orbits [2] [3]

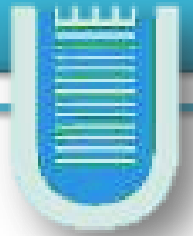
\* OUTSIDE: Lagrangian CR4BP + Low thrust,  
=> artificial non-Keplerian orbits [4]

Unit of measure  $1=10^6$  km



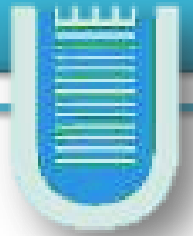






## References

- [1] April 2012: Ceccaroni, M., Biggs, J. D., Biasco, L.:  
“Analytic estimates and topological properties of the weak stability boundary”;  
Cel Mech & Dyn Astr (2012) 114:124 DOI 10.1007/s10569-012-9419-x.
- [2] November 2012: Ceccaroni, M., Biscani, F., Biggs, J. D.:  
“Analytical method for perturbed frozen orbit around an Asteroid in highly  
inhomogeneous gravitational fields. A first approximation”  
Solar System Research, Accepted for publication
- [3] November 2012: Ceccaroni, M., Biggs, J. D.: “Analytic perturbative theories  
in highly inhomogeneous gravitational fields.”  
Icarus, Accepted for publication
- [4] November 2011: Ceccaroni, M., Biggs, J. D.:  
“Low-thrust propulsion in a coplanar circular restricted four body problem”;  
Cel Mech & Dyn Astr, Volume 112, Issue 2 (2012), Page 191-219.  
DOI:10.1007/s10569-011-9391-x.



# Present

AstroNet-II project:

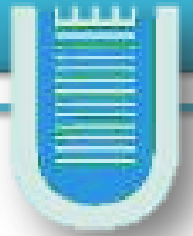
- Dissipative effects on Attitude Dynamics.
- Analytical and numerical approaches :  
perturbative and Kam theories, quasi-periodic approximations,  
Lyapunov exponents, frequency analysis and Greene's method.  
=>accurate description of the dynamics

Extend to the rotational dynamics & include dissipative effects.

periodic attractors

invariant tori

basins of attraction of the different resonances.



# Present

AstroNet-II project:

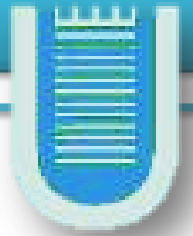
- Dissipative effects on Attitude Dynamics.
- Analytical and numerical approaches :  
perturbative and Kam theories, quasi-periodic approximations,  
Lyapunov exponents, frequency analysis and Greene's method.  
=>accurate description of the dynamics

Extend to the rotational dynamics & include dissipative effects.

periodic attractors

invariant tori

basins of attraction of the different resonances.



# Present

AstroNet-II project:

- Dissipative effects on Attitude Dynamics.
- Analytical and numerical approaches :  
perturbative and Kam theories, quasi-periodic approximations,  
Lyapunov exponents, frequency analysis and Greene's method.

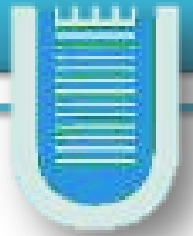
=>accurate description of the dynamics

Extend to the rotational dynamics & include dissipative effects.

periodic attractors

invariant tori

basins of attraction of the different resonances.



# Present

AstroNet-II project:

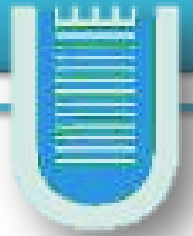
- Dissipative effects on Attitude Dynamics.
- Analytical and numerical approaches :  
perturbative and Kam theories, quasi-periodic approximations,  
Lyapunov exponents, frequency analysis and Greene's method.  
=>accurate description of the dynamics

Extend to the rotational dynamics & include dissipative effects.

periodic attractors

invariant tori

basins of attraction of the different resonances.



# Present

AstroNet-II project:

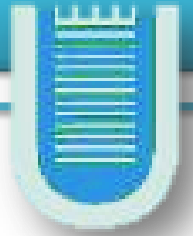
- Dissipative effects on Attitude Dynamics.
- Analytical and numerical approaches :  
perturbative and Kam theories, quasi-periodic approximations,  
Lyapunov exponents, frequency analysis and Greene's method.  
=>accurate description of the dynamics

Extend to the rotational dynamics & include dissipative effects.

periodic attractors

invariant tori

basins of attraction of the different resonances.



**Thanks for your  
attention**



**Questions?**