R. Fioresi, F. Gavarini

"On the construction of Chevalley Supergroups"

in: *Supersymmetry in Mathematics and Physics*, pp. 101–123,
S. Ferrara, R. Fioresi, V. S. Varadarajan (eds.), UCLA Los Angeles, U.S.A. 2010,
Lecture Notes in Mathematics **2027**, Springer-Verlag, Berlin-Heidelberg, 2011

— **DOI:** 10.1007/978-3-642-21744-9_5 —

the original publication is available at
`http://www.springerlink.com/content/j378521716k7204p/`

ABSTRACT

We give a description of the construction of Chevalley supergroups, providing some explanatory examples. We avoid the discussion of the $A(1,1)$, $P(3)$ and $Q(n)$ cases, for which our construction holds, but the exposition becomes more complicated. We shall not in general provide complete proofs for our statements, instead we will make an effort to convey the key ideas underlying our construction. A fully detailed account of our work is scheduled to appear in [9].

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